

# **PHYS 270 – SUPPL. #4**

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## Chapter 34. Electromagnetic Induction

Electromagnetic induction is the scientific principle that underlies many modern technologies, from the generation of electricity to communications and data storage.



# Induction

- E-fields generate B fields (E field in a conductor drives current that creates B)
- Can B fields generate E- fields?
- Yes if the B fields vary in time -Faraday

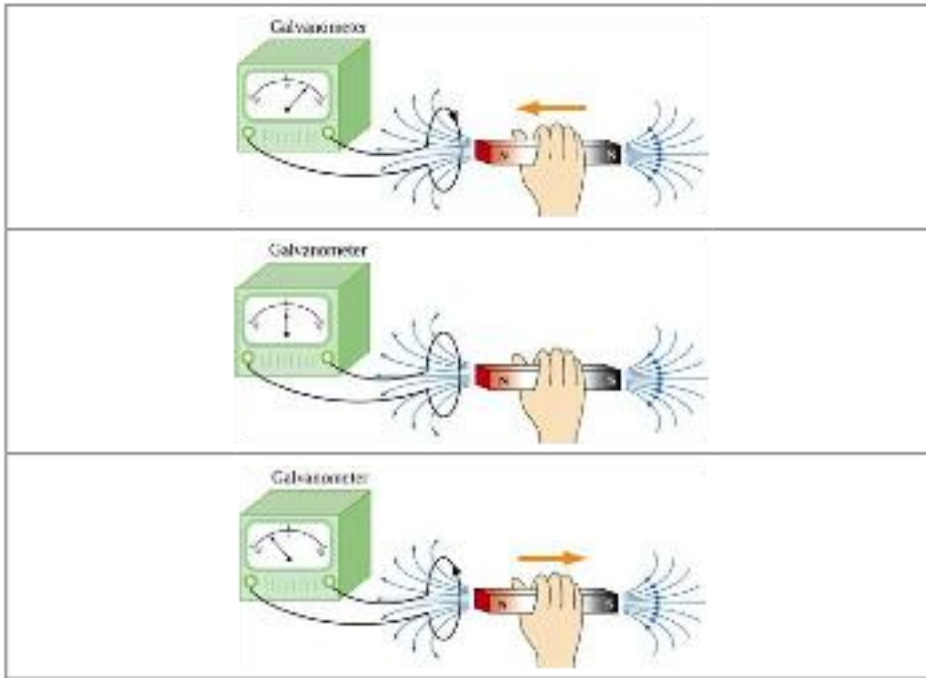


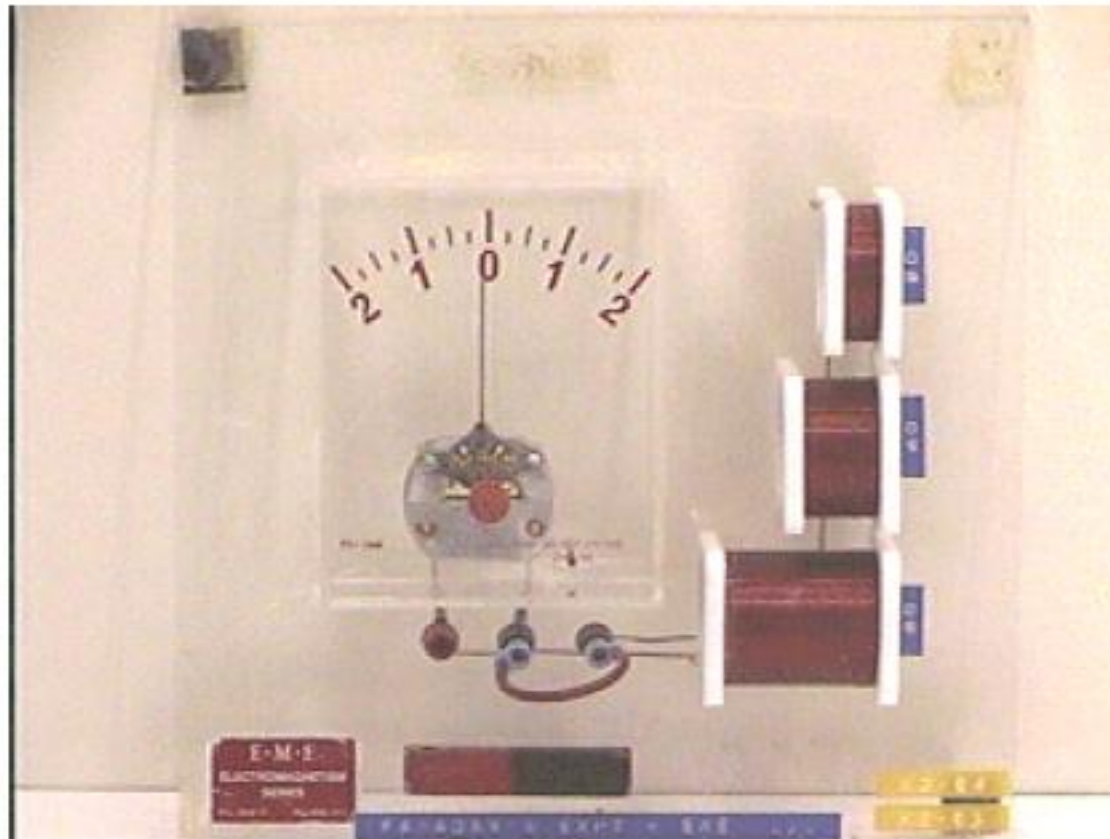
Figure 10.1.1 Electromagnetic induction

- Current flows only if B through the loop is changing
- Faster movement more current
- Current direction changes when either motion or magnet polarity is reversed
- Current linear function of number of turns

Coil behaves as connected to a battery source. EMF

$$EMF \rightarrow \mathcal{E} = -N \frac{d\Phi_m}{dt}$$

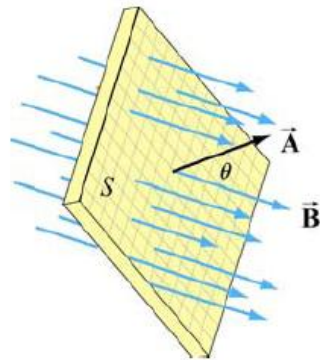
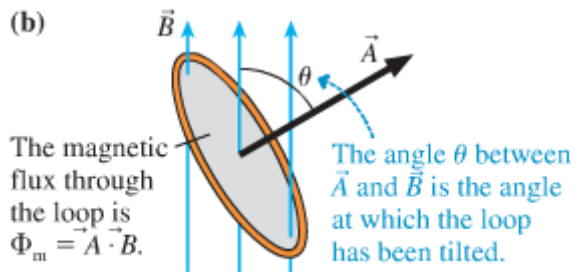
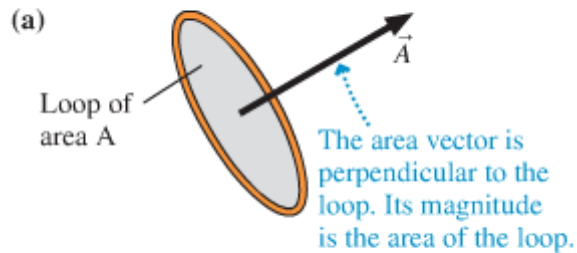
## K2-04: FARADAY'S EXPERIMENT - EME SET - 20, 40, 80 TURN COILS



# MAGNETIC FLUX CONVENTIONS

## UNIFORM B

**FIGURE 34.14** Magnetic flux can be defined in terms of an area vector.



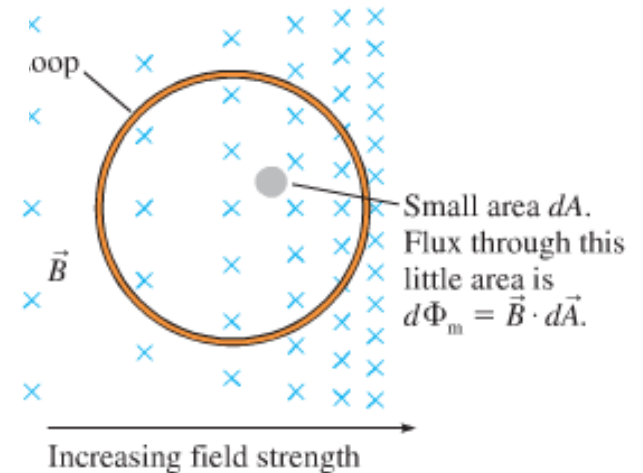
$$\Phi = AB \cos\theta$$

$$\Phi = \vec{A} \cdot \vec{B}$$

Units: T·m<sup>2</sup> = Wb (Weber)

## NON-UNIFORM B

**FIGURE 34.16** A loop in a nonuniform magnetic field.

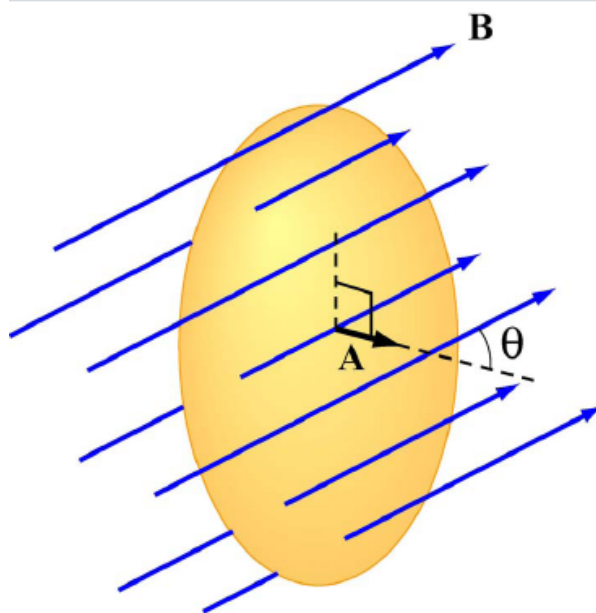


$$d\Phi = \vec{B} \cdot d\vec{A}$$

$$\Phi = \oint \vec{B} \cdot d\vec{A}$$

# Magnetic Flux Thru Wire Loop

Analogous to Electric Flux (Gauss' Law)



(1) Uniform **B**

$$\Phi_B = B_{\perp}A = BA\cos\theta = \vec{\mathbf{B}} \cdot \vec{\mathbf{A}}$$

(2) Non-Uniform **B**

$$\Phi_B = \int_S \vec{\mathbf{B}} \cdot d\vec{\mathbf{A}}$$

# Faraday's Law of Induction

$$\mathcal{E} = -N \frac{d\Phi_B}{dt}$$

A changing magnetic flux  
*induces* an EMF

## What is EMF?

$$\mathcal{E} = \int \vec{\mathbf{E}} \cdot d\vec{\mathbf{s}}$$

Looks like potential. It's a  
"driving force" for current

N number of loops  
in a coil

What about  
the minus  
sign ?

$$\varepsilon = -\frac{d}{dt}(BA\cos\theta) = -\left(\frac{dB}{dt}\right)A\cos\theta - B\left(\frac{dA}{dt}\right)\cos\theta + BA\sin\theta\left(\frac{d\theta}{dt}\right) \quad (10.1.5)$$

How can induce a emf:

1. Change magnitude of B
2. Change area A
3. Change angle  $\theta$

Thus, we see that an emf may be induced in the following ways:

(i) by varying the magnitude of  $\vec{B}$  with time (illustrated in Figure 10.1.3.)

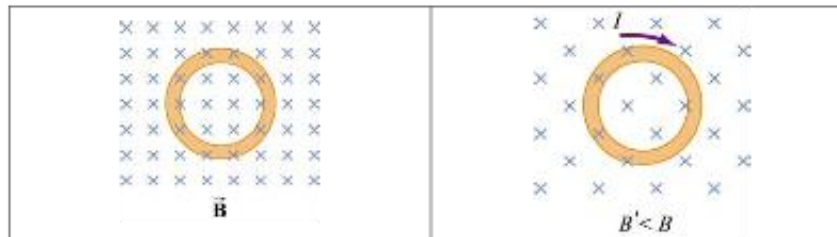


Figure 10.1.3 Inducing emf by varying the magnetic field strength

(ii) by varying the magnitude of  $\vec{A}$ , i.e., the area enclosed by the loop with time (illustrated in Figure 10.1.4.)

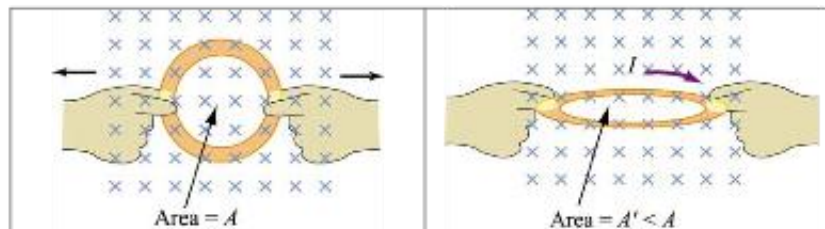


Figure 10.1.4 Inducing emf by changing the area of the loop

(iii) varying the angle between  $\vec{B}$  and the area vector  $\vec{A}$  with time (illustrated in Figure 10.1.5.)

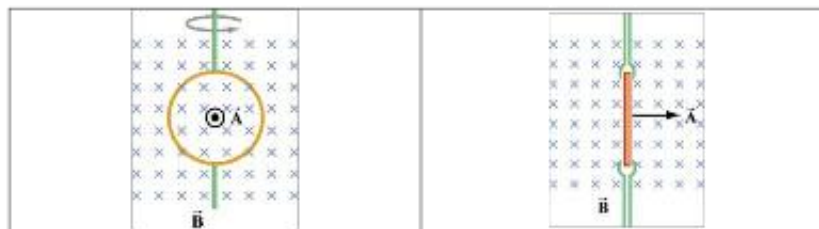
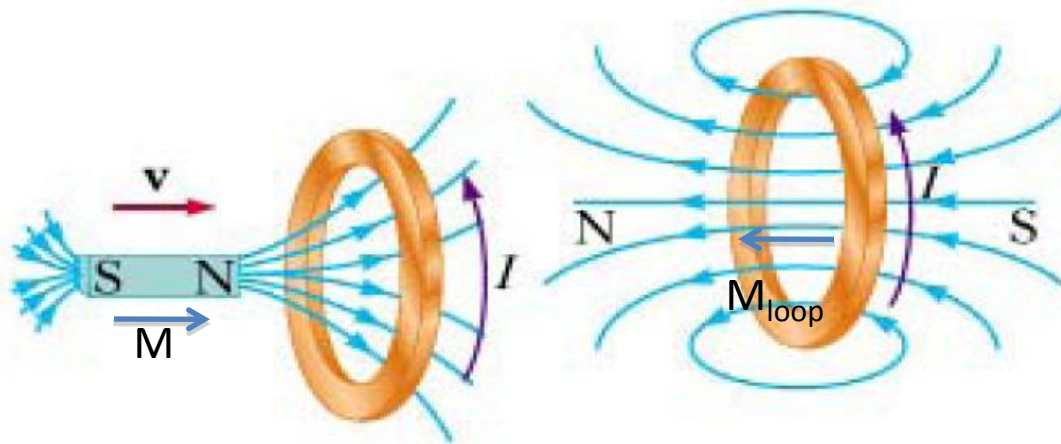


Figure 10.1.5 Inducing emf by varying the angle between  $\vec{B}$  and  $\vec{A}$ .



## Minus Sign? Lenz's Law

Induced EMF is in direction that **opposes** the change in flux that caused it



To illustrate how Lenz's law works, let's consider a conducting loop placed in a magnetic field. We follow the procedure below:

1. Define a positive direction for the area vector  $\vec{A}$ .
2. Assuming that  $\vec{B}$  is uniform, take the dot product of  $\vec{B}$  and  $\vec{A}$ . This allows for the determination of the sign of the magnetic flux  $\Phi_B$ .
3. Obtain the rate of flux change  $d\Phi_B / dt$  by differentiation. There are three possibilities:

$$\frac{d\Phi_B}{dt} : \begin{cases} > 0 \Rightarrow \text{induced emf } \mathcal{E} < 0 \\ < 0 \Rightarrow \text{induced emf } \mathcal{E} > 0 \\ = 0 \Rightarrow \text{induced emf } \mathcal{E} = 0 \end{cases}$$

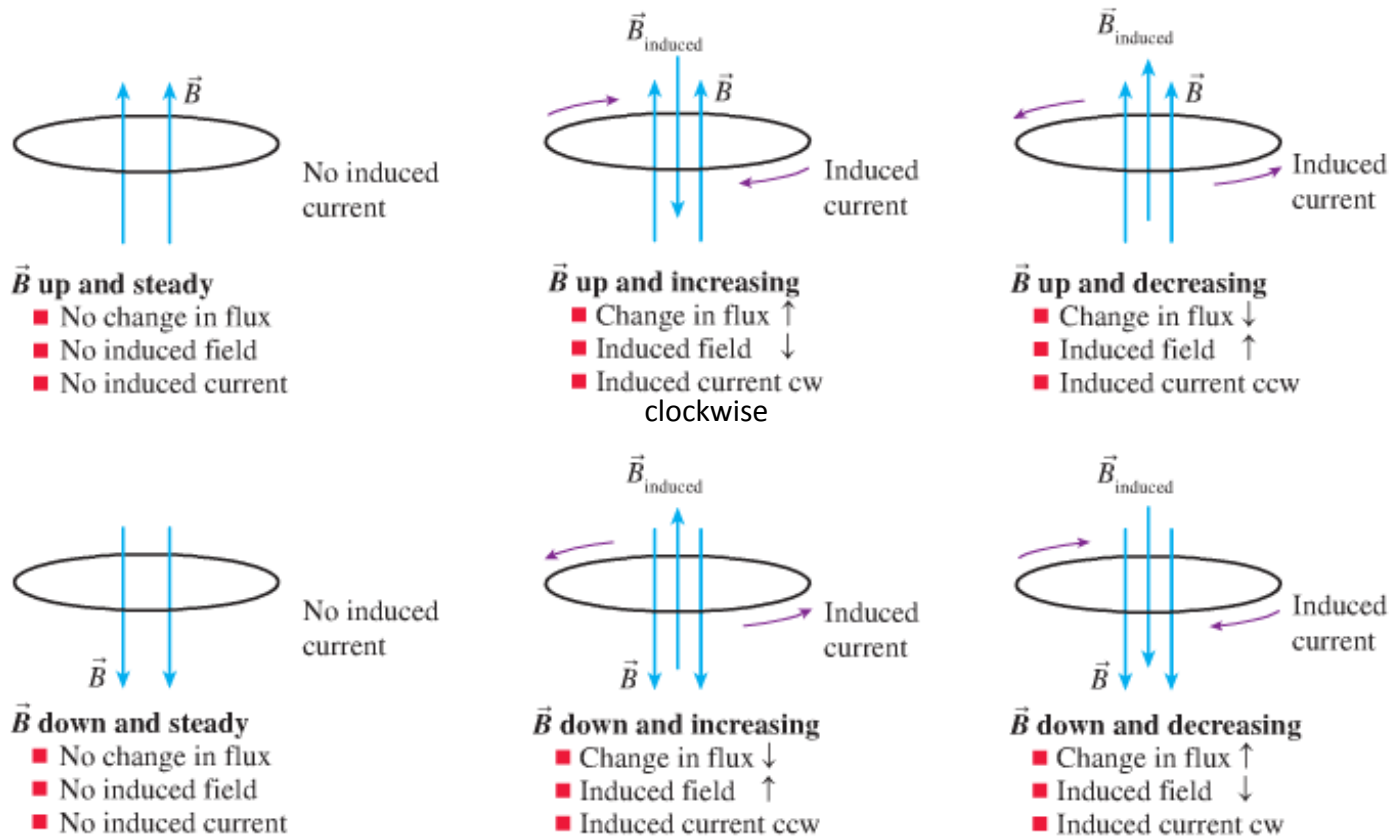
4. Determine the direction of the induced current using the right-hand rule. With your thumb pointing in the direction of  $\vec{A}$ , curl the fingers around the closed loop. The induced current flows in the same direction as the way your fingers curl if  $\mathcal{E} > 0$ , and the opposite direction if  $\mathcal{E} < 0$ , as shown in Figure 10.1.6.

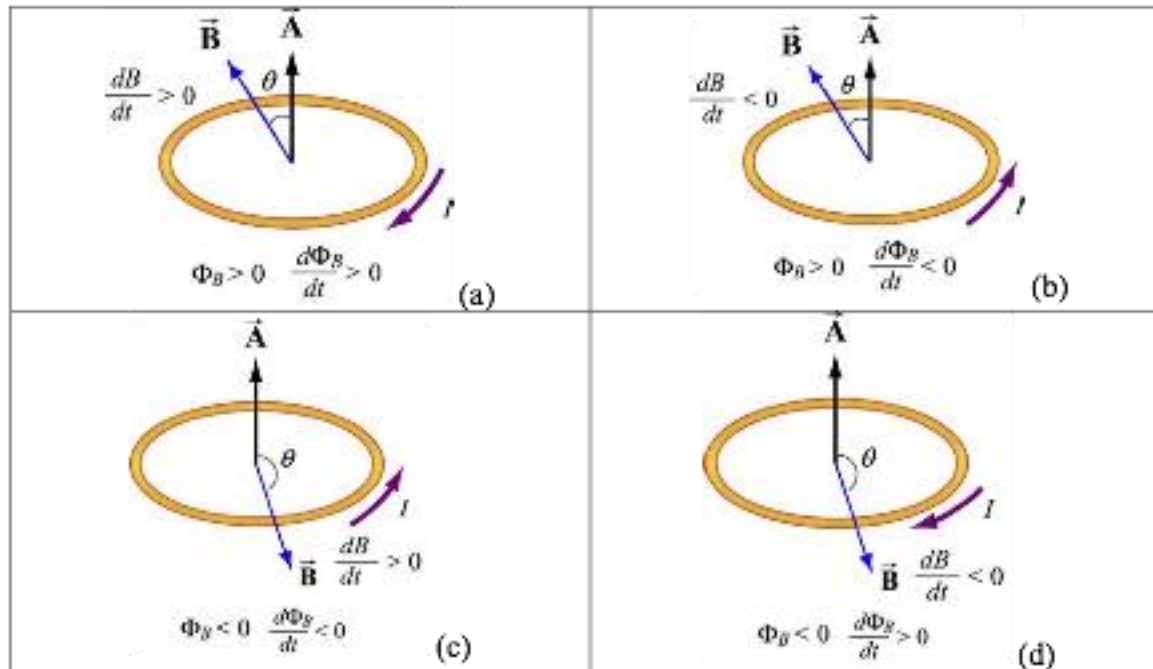


**Figure 10.1.6** Determination of the direction of induced current by the right-hand rule

# LENZ'S LAW APPLICATION

FIGURE 34.22 The induced current for six different situations.





**Figure 10.1.7** Direction of the induced current using Lenz's law

The above situations can be summarized with the following sign convention:

$\Phi_B$	$d\Phi_B / dt$	$\mathcal{E}$	$I$
+	+	-	-
	-	+	+
-	+	-	-
	-	+	+

The positive and negative signs of  $I$  correspond to a counterclockwise and clockwise currents, respectively.

# HOW TO CREATE E-FIELDS

(a) Magnetic forces separate the charges and cause a potential difference between the ends. This is a motional emf.

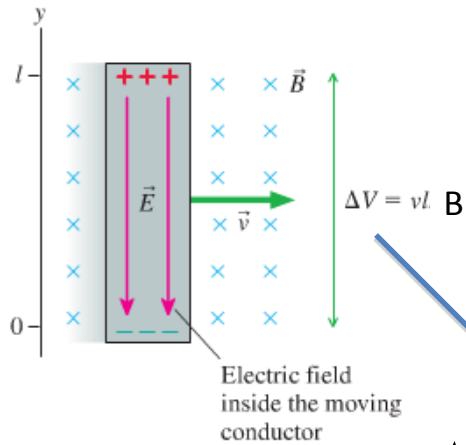
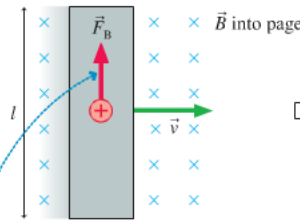
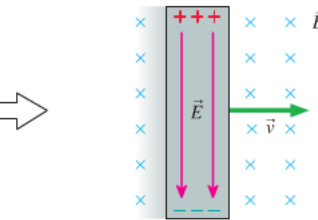


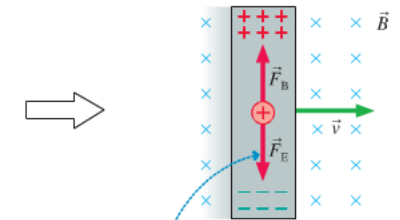
FIGURE 34.2 The magnetic force on the charge carriers in a moving conductor creates an electric field inside the conductor.



Charge carriers in the wire experience an upward force of magnitude  $F_B = qvB$ . Being free to move, positive charges flow upward (or, if you prefer, negative charges downward).

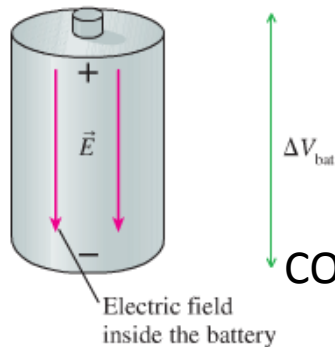


The charge separation creates an electric field in the conductor.  $E$  increases as more charge flows.



The charge flow continues until the downward electric force  $F_E$  is large enough to balance the upward magnetic force  $F_B$ . Then the net force on a charge is zero and the current ceases.

(b) Chemical reactions separate the charges and cause a potential difference between the ends. This is a chemical emf.



COULOMBIC

$$\Delta V = V_{\text{top}} - V_{\text{bottom}} = - \int_0^l E_y ds =$$

$$- \int_0^l -(vB) ds = vBl$$

$$F_E = qE$$

$$F_B = qvB$$

$$E = vB$$

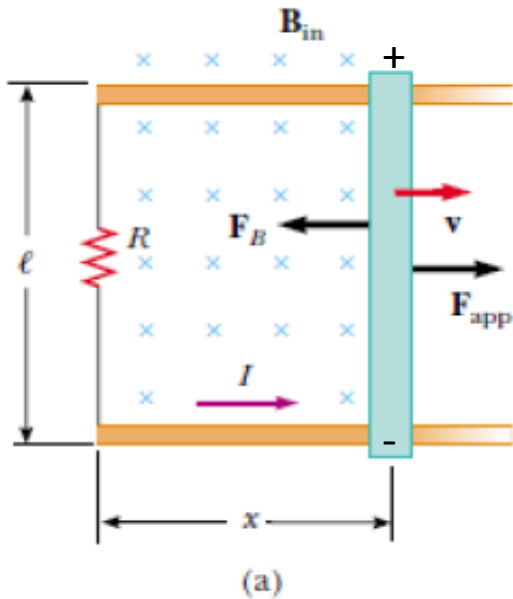
$$EMF, \mathcal{E} = v l B$$

## Motional emf

The motional emf of a conductor of length  $l$  moving with velocity  $v$  perpendicular to a magnetic field  $B$  is

$$\mathcal{E} = v l B$$

# HOW TO CREATE CURRENTS



Who provides the energy?  
What happens if I give the wire a push?

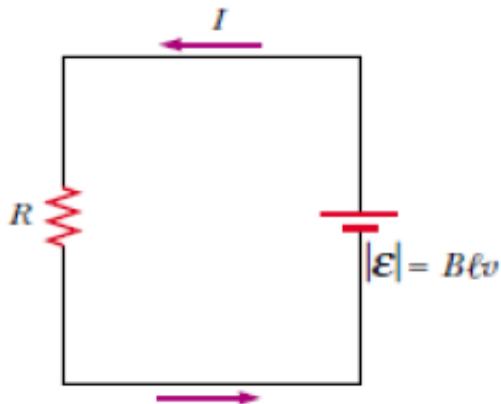
$$I = \mathcal{E} / R = v l B / R$$

$$\vec{F}_B = I(l\hat{e}_y) \times (-B\hat{e}_z) = -IlB\hat{e}_x = -\hat{e}_x \left( \frac{B^2 l^2 v}{R} \right)$$

$$m \frac{dv}{dt} = F_B = -\frac{B^2 l^2 v}{R}$$

$$dv / v = -\frac{B^2 l^2 v}{mR} dt = -dt / \tau$$

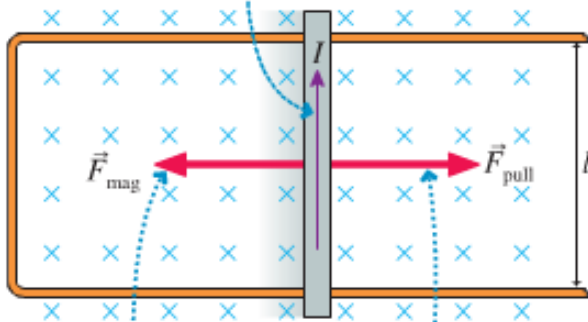
$$v(t) = v(t=0) \exp(-t / \tau)$$



# ENERGY – POWER ISSUES

**FIGURE 34.6** A pulling force is needed to move the wire to the right.

The induced current flows through the moving wire.



The magnetic force on the current-carrying wire is opposite the motion.

A pulling force to the right must balance the magnetic force to keep the wire moving at constant speed. This force does work on the wire.

$$dW = \vec{F} \cdot d\vec{s}$$

$$P = dW / dt = \vec{F} \cdot (d\vec{s} / dt) = \vec{F} \cdot \vec{v}$$

To maintain constant  $\vec{v}$  need to apply a force

$$\vec{F}_{\text{pull}} = e_x IlB = e_x (v l B / R) l B$$

$$P_{\text{inp}} = \frac{(v l B)^2}{R}$$

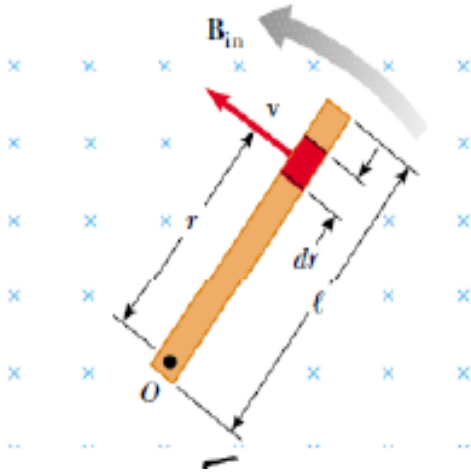
$$P_{\text{diss}} = I^2 R = \frac{(v l B)^2}{R}$$

Energy  
Conservation

A simple generator transforms mechanical power to electrical power



## Rotating conducting bar in magnetic field



A conducting bar of length  $\ell$  rotates with a constant angular speed  $\omega$  about a pivot at one end. A uniform magnetic field  $\mathbf{B}$  is directed perpendicular to the plane of rotation, as shown in Figure 31.11. Find the motional emf induced between the ends of the bar.

Let  $dq$  be charge within element  $dr$   
In equilibrium:

$$F_E = F_B \rightarrow dq dE = dq v B$$

$dE$  parallel to the bar and across  $dE$

$$v = \omega r \rightarrow dE = \omega r B$$

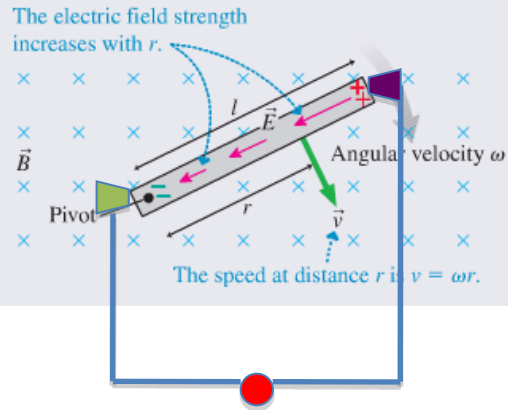
For uniform  $E$  - field  $\rightarrow |\Delta V| = Ed$

$$dV = dE dr = \omega B r dr$$

$$\Delta V = \omega B \int_0^l r dr = \frac{1}{2} \omega B l^2$$

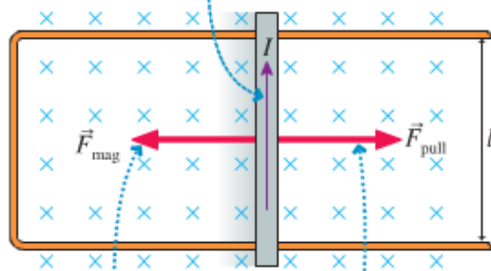
Hydroelectric Power

**FIGURE 34.4** Pictorial representation of a metal bar rotating in a magnetic field.



**FIGURE 34.6** A pulling force is needed to move the wire to the right.

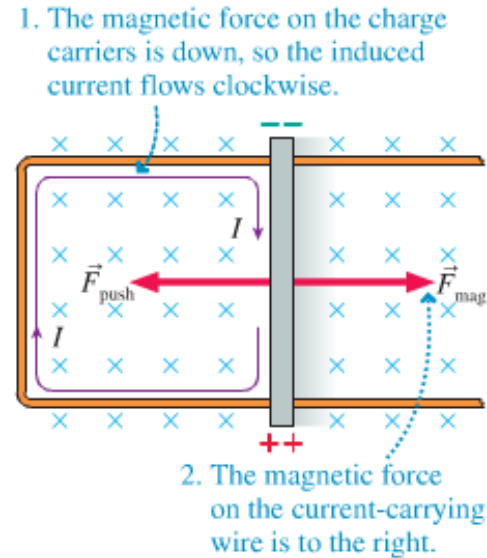
The induced current flows through the moving wire.



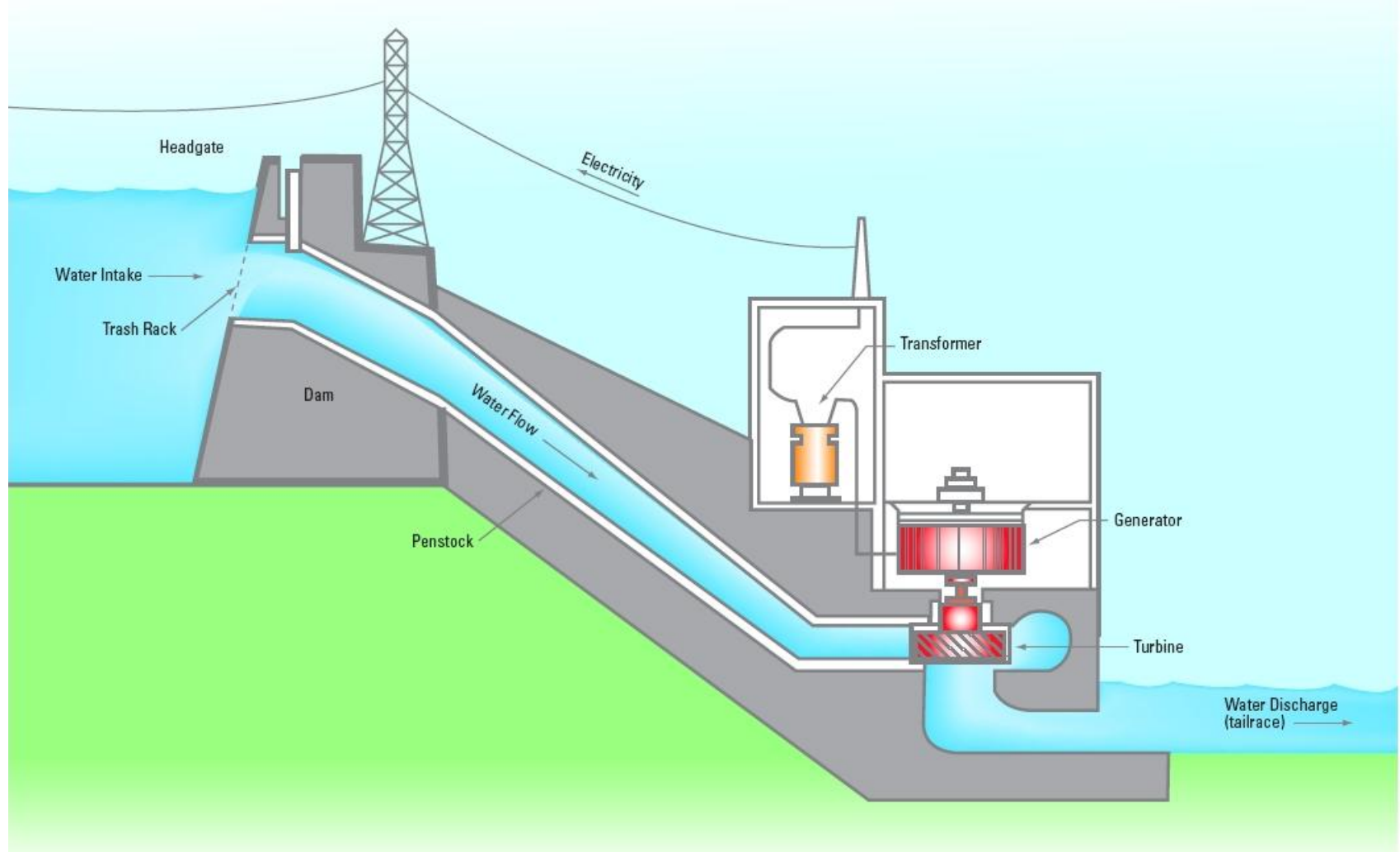
The magnetic force on the current-carrying wire is opposite the motion.

A pulling force to the right must balance the magnetic force to keep the wire moving at constant speed. This force does work on the wire.

**FIGURE 34.7** A pushing force is needed to move the wire to the left.

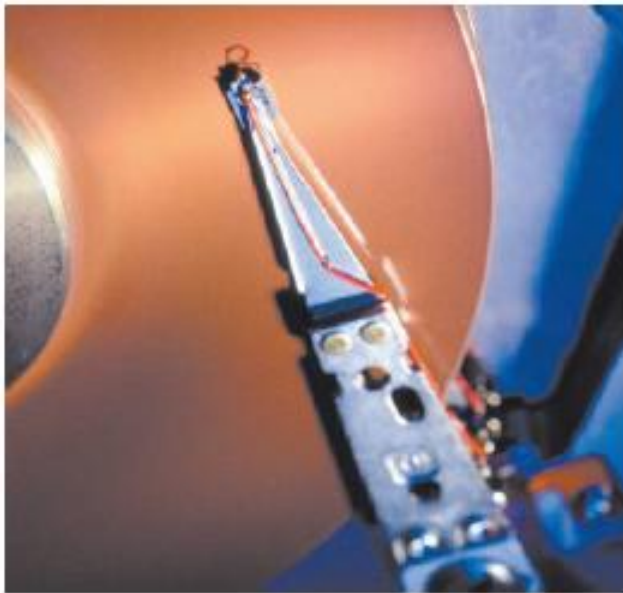
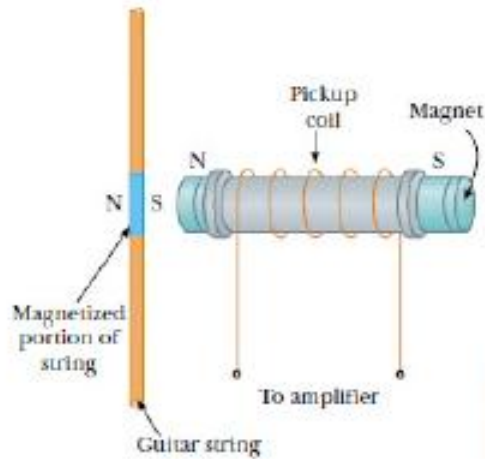


# Hydro-Electric Station



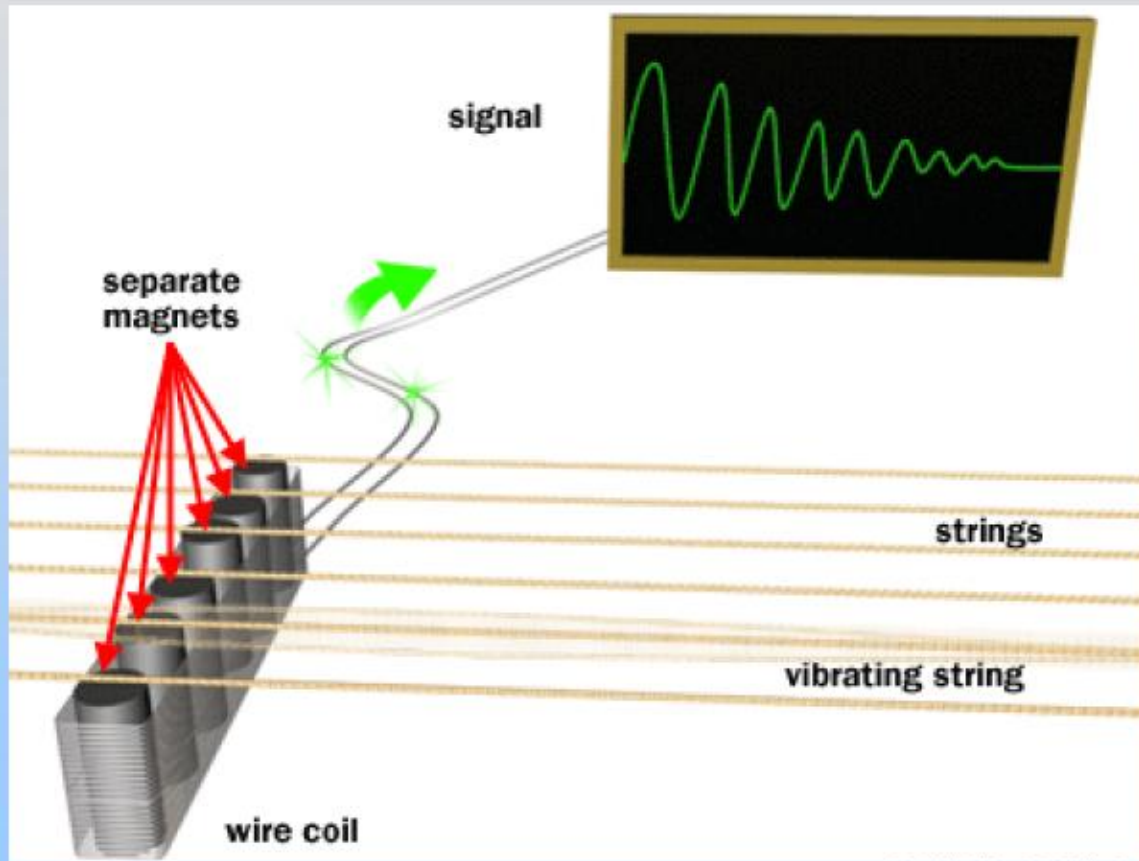
Watch movie at

[www.opg.com/power/hydro/howitworks.asp](http://www.opg.com/power/hydro/howitworks.asp)



Magnetic data storage encodes information in a pattern of alternating magnetic fields. When these fields move past a small *pick-up coil*, the changing magnetic field creates an induced current in the coil. This current is amplified into a sequence of voltage pulses that represent the 0s and 1s of digital data.

# Electric Guitar



P20-41

# TETHERED SATELLITE SYSTEM

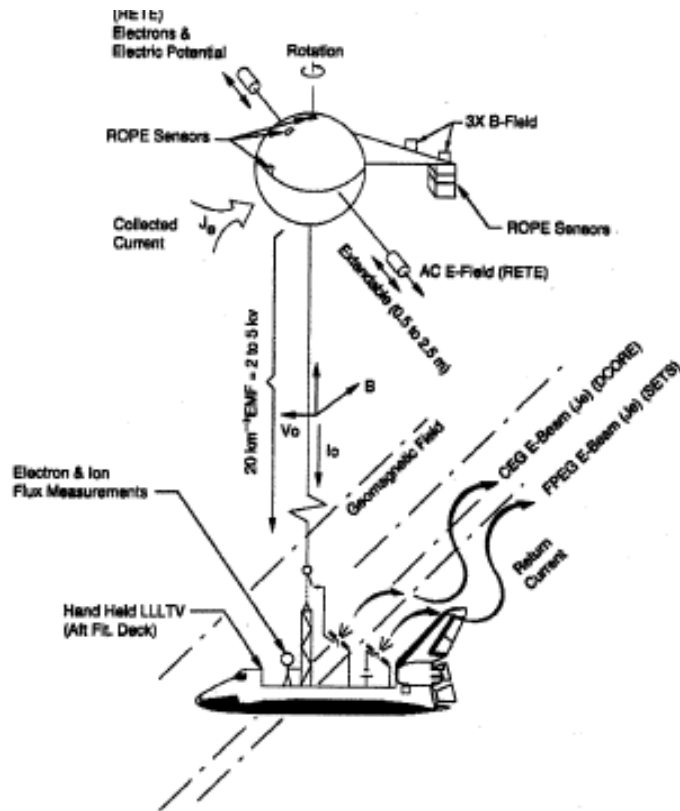


Figure 1.6 TSS Functional Schematic

$$EMF = vIB = (8 \text{ km/sec}) (20 \text{ km}) (.3 \times 10^{-4} \text{ T}) = 4.8 \text{ kV}$$

$$R = 4.8 \text{ kV} / 1\text{A} = 4800 \text{ Ohm}$$

$$P = I(EMF) = 4.8 \text{ kW}$$

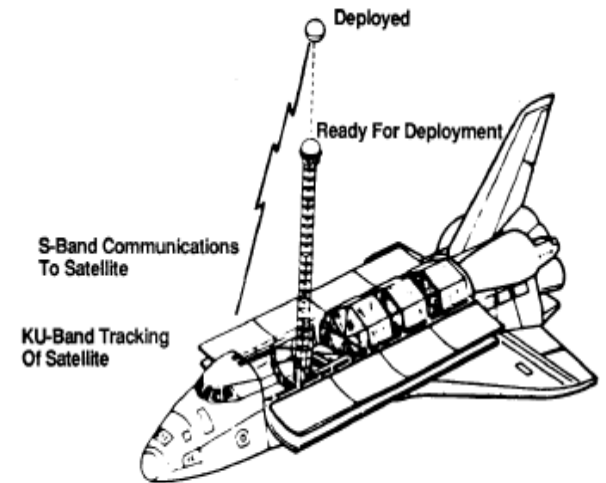


Figure 1.1 TSS-1 Satellite and Tether Attached to 12 Meter Extendible Boom

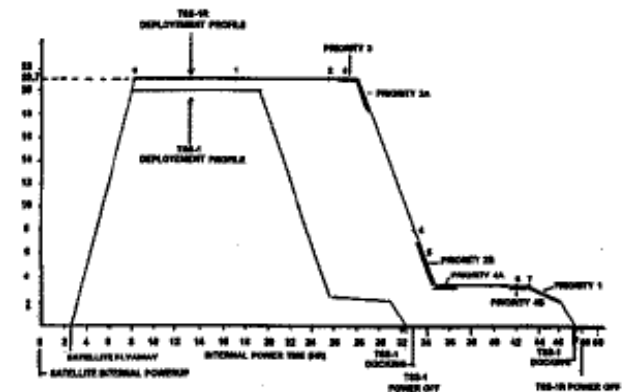


Figure 1.3 TSS1 and TSS1R Timelines